

## LONE-PAIR CHARGES AND STRUCTURAL EFFECTS

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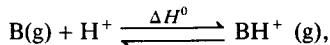
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The lone-pair charge,  $Q_{lpf}$ , of a base B is a (theoretically calculated) measure of the amount of charge on the lone pair of B that binds to an acid A' ( $\nu = 0, 1$ ) in an acid-base reaction. It is shown how they can be used for the quantitative study of structural effects on gas-phase proton affinities, vertical ionization potentials and hydrogen-bonding basicities.

## INTRODUCTION

The systematic development of experimental and theoretical gas-phase ion chemistry<sup>1-8</sup> in the last 10 years has led to a rapid accumulation of information and it is now possible to analyse *a posteriori* a substantial body of different experimental data relating to the Lewis concept of basicity.

Special attention has been paid to the study of substituent effects.<sup>5</sup> *Ab initio* SCF calculations provide useful information on the role played by substituents on the structure and reactivity of a given system.<sup>6,7</sup> A considerable number of linear relationships between gas-phase proton affinities [defined as  $PA = -\Delta H^0$  for the process



where B is a base] and some theoretical indices have been proposed.<sup>6</sup> Energy-charge correlations have been especially useful in reactivity studies.

It is usually accepted that some characteristics of a basic centre are correlated with its gas-phase PA. One of these characteristics is the charge on the lone pair involved in the formation of the corresponding cation on protonation. It has been shown<sup>9</sup> that the electronic population of the basic centre bears only a rough relationship with the energy variation of the corresponding proton-transfer equilibrium.

In previous work an economical way to evaluate the lone-pair charge in an SCF procedure was proposed.<sup>8-11</sup> The lone-pair-charge ( $Q_{lpf}$ ) concept reflects the interest in finding theoretical methods that allow the prediction of structural effects on basicity. It has been shown<sup>8-11</sup> that the gas-phase proton affinities of a wide variety of organic bases are linear functions of the  $Q_{lpf}$  values of their protonation sites.

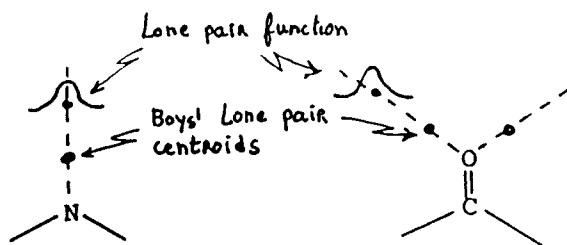
We report here that a series of compounds exists for which this simple linear relationship breaks down, and

show how this failure provides a new and powerful tool for the analysis of molecular properties.

## COMPUTATIONAL DETAILS

For compatibility with our previous studies<sup>8-11</sup> we carried out *ab initio* calculations at the minimal basis set level following the model employed previously based on fully optimized INDO geometries, where the CH, NH and OH bond lengths were conveniently scaled to account for the fact that the INDO method overestimates them. The scaling factors for CH (0.974), NH (0.935) and OH (0.924) bond lengths are the ratios of the experimental CH bond lengths in naphthalene, NH bond lengths in pyrrole and OH bond lengths in phenol, respectively, to the INDO optimized values.

The lone-pair charge is evaluated using a lone-pair function (LPF) formed by one s-type and three p-type ( $x, y, z$ ) Gaussian-type orbitals (GTOs) with identical exponents and centred at the same point in space. This basis (to be added to the STO-3G<sup>12</sup> minimal basis set) is located on the line that joins the basic centre (either N or O) to the centroid of charge of the corresponding Boys' localized<sup>13</sup> lone-pair orbital (see Scheme 1) from a previous STO-3G calculation. The charge on the LPF is evaluated using the well known Mulliken population method.



Scheme 1

The previously reported<sup>8</sup> values of exponents (0.10) and position (0.85 Å away from the N atom) are used in this work, when N is the basic centre. Following the same methodology as given in Ref. 8 and taking benzaldehyde as a probe, we obtained for compounds in which O is the basic centre exponent = 0.133 and position 0.773 Å away from the O atom.

We have proved<sup>8</sup> that the basis set STO-3G + LPF does not present any abnormal behaviour.

All the calculations were performed at UAM/IBM Scientific Centre and CC/UAM Centre in Madrid using the programs GEOMO<sup>14</sup> and our version of GAUSSIAN 80<sup>15</sup> (IBM MVS version by E. M. Fluder and L. R. Kahn, modified by us to run under VM/CMS).

## RESULTS AND DISCUSSION

Table 1 shows the relative proton affinities,  $\delta\text{PA}$  [i.e. the standard enthalpy changes, for reaction (1) in the gas phase] for *para*-substituted benzaldehydes (Data from Ref. 16 except for 4-NH<sub>2</sub> value, kindly communicated by Prof. R. W. Taft) (Y = H, series I) and acetophenones<sup>17</sup> (Y = CH<sub>3</sub>, series II). Also given are calculated  $Q'_{\text{lpf}}$  values for the lone pairs of their carbonyl oxygens.

Table 1. Relative gas-phase proton affinities ( $\delta\text{PA}$ ), vertical ionization potentials (VIP) and lone-pair charges ( $Q'_{\text{lpf}}$  and  $Q'_{\text{lpf}}$ ) for 4-X-substituted benzaldehydes and acetophenones

X	Y	$\delta\text{PA}$ (kcal mol <sup>-1</sup> ) <sup>16,17</sup>	VIP (kcal mol <sup>-1</sup> ) <sup>18</sup>	$Q'_{\text{lpf}}$ (electron units)	$Q'_{\text{lpf}}$ (electron units)
N(CH <sub>3</sub> ) <sub>2</sub>	H	21.1	216.8	0.3732	0.3804
NH <sub>2</sub>	H	14.9	219.7 <sup>b</sup>	0.3689	0.3736
OCH <sub>3</sub>	H	10.2	224.9	0.3629	0.3675
OH	H	6.9	223.7 <sup>b</sup>	0.3628	0.3643
CH <sub>3</sub>	H	4.5	225.6	0.3578	0.3593
F	H	-0.6	227.2	0.3563	0.3556
H	H	(0)	228.1	0.3554	0.355
Cl	H	-0.5	231.8	0.3494	—
CHO	H	-4.5 <sup>a</sup>	232.0 <sup>b</sup>	0.3493	0.3503
CF <sub>3</sub>	H	-5.9	235.3 <sup>b</sup>	0.3442	0.3472
CN	H	-8.0	238.7	0.3436	0.3448
NO <sub>2</sub>	H	-8.7	239.2	0.3382 <sup>c</sup>	0.3430
N(CH <sub>3</sub> ) <sub>2</sub>	CH <sub>3</sub>	18.1	208.4 <sup>b</sup>	0.3938	0.4013
NH <sub>2</sub>	CH <sub>3</sub>	11.4	209.4	0.3924	0.3957
OCH <sub>3</sub>	CH <sub>3</sub>	8.1	212.2	0.3869	0.3900
OH	CH <sub>3</sub>	5.4	213.3 <sup>b</sup>	0.3865	0.3874
CH <sub>3</sub>	CH <sub>3</sub>	3.9	216.3	0.3834	0.3835
F	CH <sub>3</sub>	-0.6	217.4 <sup>b</sup>	0.3805	0.3797
H	CH <sub>3</sub>	(0)	219.3	0.3797	0.380
Cl	CH <sub>3</sub>	-0.7	219.6	—	—
CHO	CH <sub>3</sub>	-4.5	221.8	0.3731	0.3747
CN	CH <sub>3</sub>	-8.2	226.5	0.3682	0.3689
NO <sub>2</sub>	CH <sub>3</sub>	-8.8	230.2	0.3624	0.3675

<sup>a</sup>Calculated from the excellent linear relationship between ( $\delta\text{PA}$ )<sub>I</sub> and ( $\delta\text{PA}$ )<sub>II</sub> given in Ref. 17.

<sup>b</sup>Calculated from the excellent linear relationship found between the experimental VIPs and the STO-3G calculated energies of the  $n_0$  orbitals (see Table 2).

<sup>c</sup> $Q'_{\text{lpf}}$  for the 3-NO<sub>2</sub> derivative is 0.3385 electrons.

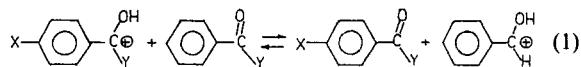
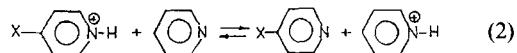


Figure 1 shows plots of  $\delta\text{PA}$  vs  $Q'_{\text{lpf}}$  for series I and II. The  $Q'_{\text{lpf}}$  calculated for 4-substituted pyridines taken from Ref. 9 are shown for comparison purposes (series III in Figure 2).  $\delta\text{PAs}$  for these compounds were taken from Ref. 5 and are defined according to reaction (2).



It appears that in all three cases, +R (electron-acceptor) and -R (electron-donor) substituents define two different lines, the ratios  $\xi = S_{-R}/S_{+R}$  of their slopes (S) being  $\xi_I = 2.42 \pm 0.27$ ,  $\xi_{II} = 2.19 \pm 0.73$  and  $\xi_{III} = 1.29 \pm 0.35$  (excluding the 4-F value,  $\xi_{III} = 1.16 \pm 0.29$ ).

The same applies to vertical ionization potentials (VIP).<sup>18</sup> In Figure 3 the VIPs for the  $n_0$  orbitals of the carbonyl oxygen (for some compounds experimental values were estimated from the excellent linear relationships between experimental VIPs and the STO-3G energies of the  $n_0$  orbitals; see Table 2) are plotted against  $Q'_{\text{lpf}}$ . The linear relationships are excellent ( $r^2$  and standard deviations in the ranges 0.974–0.992 and

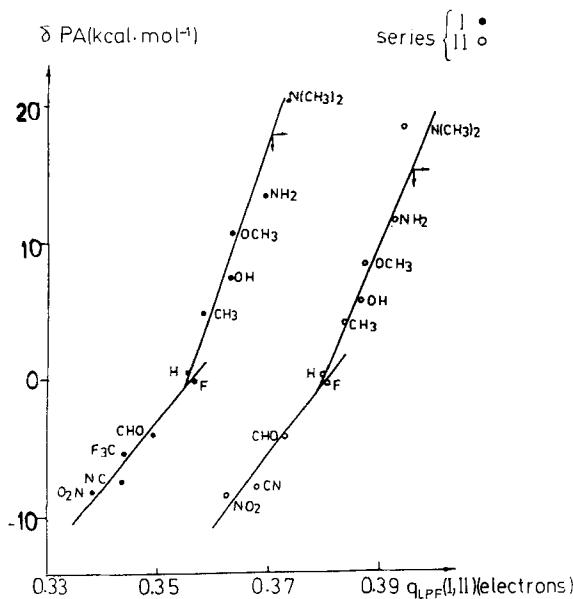


Figure 1. Relative proton affinities ( $\delta PA$ ) for series I and II (benzaldehydes and acetophenones) vs. calculated lone-pair charges ( $Q_{Lpf}$ )

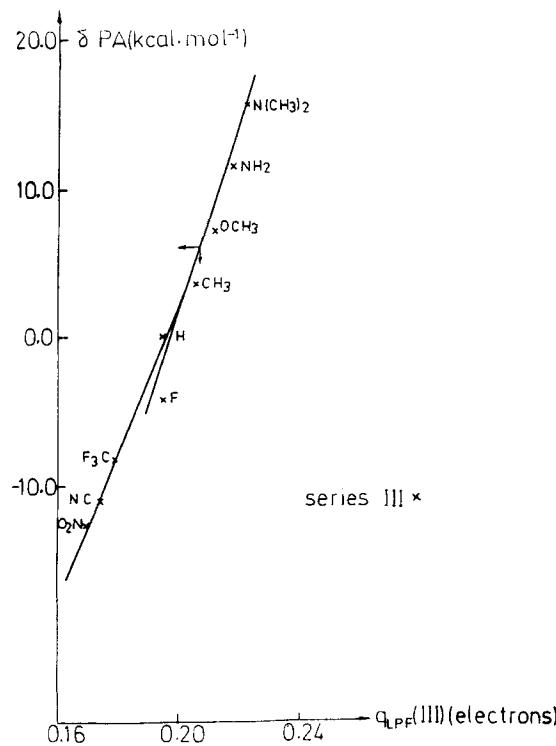


Figure 2. Relative proton affinities ( $\delta PA$ ) for series III (pyridines) vs. calculated lone-pair charges ( $Q_{Lpf}$ )

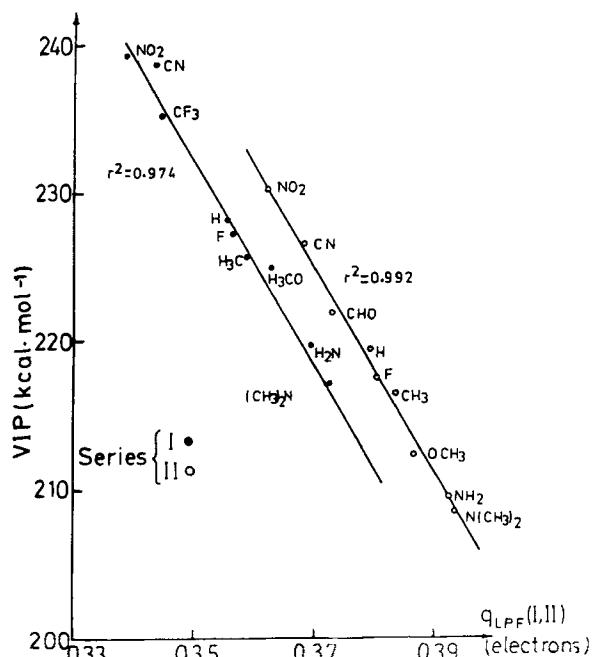


Figure 3. Vertical ionization potentials (VIP) for series I and II (benzaldehydes and acetophenones) vs. calculated  $Q_{Lpf}$  values

0.5–1.0 kcal mol<sup>-1</sup>, respectively). As expected, the plots of  $\delta PA$  vs VIP are bilinear. This is to be compared with the highly precise linear relationships that exist between PAs and adiabatic ionization potentials.<sup>19</sup>

Little electron demand is involved in hydrogen-bonding processes in which proton transfer is not a significant contributor.<sup>20</sup> The charge involved in hydrogen-bonding processes is much lower than in protonation processes. We may expect a better description using  $Q_{Lpf}$ . Some relative standard free energies,  $\delta\Delta G_{HB}^0$ , for the formation of 1:1 complexes between substituted benzaldehydes or acetophenones and phenol (ArOH) in CCl<sub>4</sub> or C<sub>2</sub>Cl<sub>4</sub> solutions at 25.0 °C [reaction (3)] are available. ( $\delta\Delta G_{HB}^0$  is calculated from equilibrium constants at 298 K in the concentration scale, taken from Ref. 21. For related compounds, the  $\delta\Delta G_{HB}^0$  values closely follow the ranking of  $\delta\Delta H_{HB}^0$  values.<sup>22</sup>) We have represented this in Figure 4, which shows that  $\delta\Delta G_{HB}^0$  values are indeed linear, with  $r^2 = 0.971$  for series I (*para*-substituted benzaldehydes) and  $r^2 = 0.988$  for series II (*para*-substituted acetophenones).  $Q_{Lpf}$  is thus a means of describing hydrogen-bonding free energies.

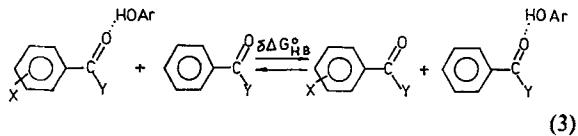
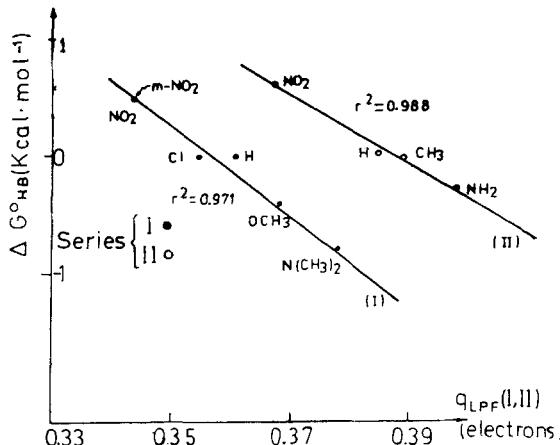


Table 2. STO-3G oxygen lone-pair energies ( $\epsilon_{\text{lo}}$ ) and experimental vertical ionization potentials (VIP)<sup>18</sup> in kcal mol<sup>-1</sup> for *para*-substituted benzaldehydes and acetophenones<sup>a,b</sup>

Benzaldehydes	Exp.	STO-3G	Acetophenones	Exp.	STO-3G
$\text{N}(\text{CH}_3)_2$	216.8	205.1	$\text{NH}_2$	209.4	201.0
$\text{O}(\text{CH}_3)$	224.9	210.3	$\text{O}(\text{CH}_3)$	212.2	204.9
$\text{CH}_3$	225.6	211.4	$\text{CH}_3$	216.3	206.0
F	227.2	214.9	H	219.3	207.6
H	228.1	213.3	CHO	221.6	214.0
Cl	231.8	220.5	CN	226.5	219.2
CN	238.7	225.2	$\text{NO}_2$	230.2	222.9
$\text{NO}_2$	239.2	229.2			

<sup>a</sup> Benzaldehydes:  $\text{VIP} (\text{kcal mol}^{-1}) = 0.8981 (-\epsilon_{\text{lo}}) + 34.83; r = 0.9785$ Acetophenones:  $\text{VIP} (\text{kcal mol}^{-1}) = 0.9300 (-\epsilon_{\text{lo}}) + 22.83; r = 0.992$ .<sup>b</sup> Calculated oxygen lone-pair energies at STO-3G level:benzaldehydes:  $\text{NH}_2$  205.0, OH 210.2, CHO 219.5,  $\text{CF}_3$  223.2 kcal mol<sup>-1</sup>;  
acetophenones:  $\text{N}(\text{CH}_3)_2$  199.5, OH 209.2, F 204.8 kcal mol<sup>-1</sup>.Figure 4. Relative standard free energies ( $\delta\Delta G_{\text{HB}}^0$ ) [reaction (3)] for series I and II (benzaldehydes and acetophenones) vs. calculated  $Q_{\text{ipf}}$  values

The substituent effects on the PAs may be separated<sup>5</sup> into three contributions:

$$\delta\Delta G = R + P + F = \rho_R \sigma_R + \rho_P \sigma_P + \rho_F \sigma_F$$

where  $R$ ,  $P$  and  $F$  are the contributions of the resonance, polarizability and field effects, respectively. A quantitative analysis of substituent effects on the  $\delta\text{PAs}$  of series I, II and III<sup>5</sup> shows that the importance of the resonance effect increases in the order

III < II < I (see Table 3). This is also the order of increasing electron demand on the corresponding protonated systems.

A similar analysis of  $Q_{\text{ipf}}$  will indicate how substituents contribute to this value and also how substituents transmit their effect ( $\rho$ ). For this analysis we employ the corresponding  $\sigma_R$  for neutral molecules, which we define as the arithmetic mean of the corresponding values for acid-base equilibria in cationic and anionic systems. Data are taken from Ref. 5.

Using multivariate regression analysis the following were obtained:

#### Benzaldehydes:

$$Q_{\text{ipf}} = 0.3537 - 0.040\sigma_R - 0.020\sigma_F - 0.004\sigma_P \quad (4)$$

$$(n = 11, r = 0.993)$$

#### Acetophenones:

$$Q_{\text{ipf}} = 0.3801 - 0.035\sigma_R - 0.020\sigma_F - 0.002\sigma_P \quad (5)$$

$$(n = 10, r = 0.994)$$

#### Pyridines:

$$Q_{\text{ipf}} = 0.1953 - 0.060\sigma_R - 0.0347\sigma_F - 0.008\sigma_P \quad (6)$$

$$(n = 9, r = 0.997)$$

After establishing the transmittance factors of these effects ( $\rho_R$ ,  $\rho_F$  and  $\rho_P$ ), we can find the values of  $Q_{\text{ipf}}$  that will correspond to our studied series of compounds if they showed cationic behaviour, i.e. the calculated lone-pair charge ( $Q'_{\text{ipf}}$ ) corresponding to the use in equa-

Table 3. Comparison between  $\rho_R$  and  $\rho_F$  taken from Ref. 5 and the calculated ratio  $\xi = S_{-R}/S_{+R}$ 

Series	Compounds	$\rho_R$	$\rho_F$	$\rho_R/\rho_F$	$\xi = S_{-R}/S_{+R}$
I	Benzaldehydes	$31.6 \pm 0.7$	$16.6 \pm 0.6$	1.90	2.42
II	Acetophenones	$27.4 \pm 0.5$	$16.1 \pm 0.5$	1.70	2.19
III	Pyridines	$25.7 \pm 0.6$	$21.8 \pm 0.6$	1.18	1.29

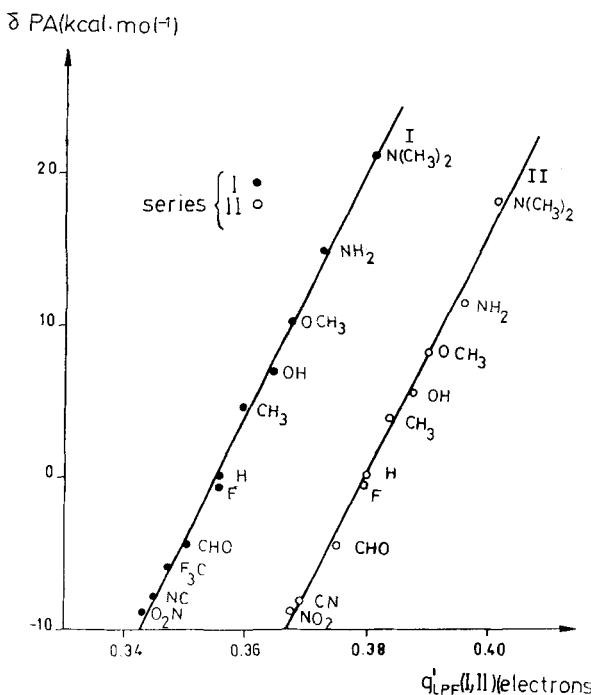
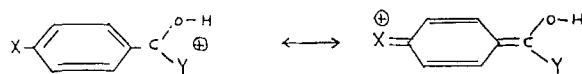


Figure 5. Relative proton affinities ( $\delta PA$ ) for series I and II (benzaldehydes and acetophenones) vs. calculated  $A'_{lpf}$  values

tions (4) and (5) of the  $\sigma_R$  values reported in Ref. 5 for cationic systems.

Following this procedure, we obtained the values of  $Q'_{lpf}$  shown in the last column in Table 1. Figure 5 shows a plot of  $Q'_{lpf}$  vs  $\delta PA$  in the gas phase. There is an excellent agreement and the plot is linear ( $r = 0.997$ ,  $r = 0.996$ ).

As  $Q'_{lpf}$  is calculated on neutral molecules, it is not able to reproduce completely  $\pi$ -donor effects in the positively charged protonated form<sup>23</sup> and it may explain the ranking of the  $\xi$  values, namely  $\xi_I < \xi_{II} < \xi_{III}$ . Our multivariate analysis of  $Q'_{lpf}$  shows that  $Q'_{lpf}$  will reproduce this effect.



### CONCLUSIONS

There is a proportionality between basicity (proton affinity) and the electronic charge density that the system is able to place on the basic centre ( $Q'_{lpf}$ ). Also the amount of this charge can change depending on the electron demand of the attacking acid (gas-phase basicity  $H^+$ ; hydrogen-bonding basicity  $RH^{\delta+}$ , etc.).

The present findings confirm that the lone-pair charge formalism is a reliable tool for the study of substituent effects, and can be used for the quantitative study of

structural effects on  $\delta PA$ , vertical ionization potentials and hydrogen-bonding basicities as shown Figures 1-5.

### ACKNOWLEDGEMENT

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